

Representational Format and Universal Quantifiers

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Introduction: First- & second-order meanings

Big Picture Question: How are universal quantifiers – each, every, and all – mentally represented?

- Finding: Despite truth-conditional equivalence, *each* biases representing individuals; *every/all* bias representing groups
- Conclusion: Even though all three universals are first-orderizable, only *each* has a first-order representation

First- vs. second-order quantification

- There are infinitely many ways to formally specify the relation expressed by universal quantifiers, including (1)-(4)

“every dot is blue”

$\left. \begin{array}{l} (1) \lambda D. \lambda B. \forall x: Dx[Bx] \\ (2) \lambda D. \lambda B. \exists x: Dx[\neg Bx] \\ (3) \lambda D. \lambda B. D \subseteq B \\ (4) \lambda D. \lambda B. D = D \cap B \\ (5) \dots \end{array} \right\}$	$\left. \begin{array}{l} (1) \lambda D. \lambda B. \forall x: Dx[Bx] \\ (2) \lambda D. \lambda B. \exists x: Dx[\neg Bx] \end{array} \right\}$	First-order: domain=individuals; assignment=one value per variable
	$\left. \begin{array}{l} (3) \lambda D. \lambda B. D \subseteq B \\ (4) \lambda D. \lambda B. D = D \cap B \\ (5) \dots \end{array} \right\}$	Second-order: genuine relation between two groups / sets

- Are the universals equally-well described by (1)-(4)? Or are meanings specified at a finer grain-size in the mind?

Linking Hypothesis:

- People are biased toward verification strategies that transparently reflect the meaning under evaluation [1-3]
 - Methodological strategy: Variation in verification that can't be otherwise explained is due to the meaning

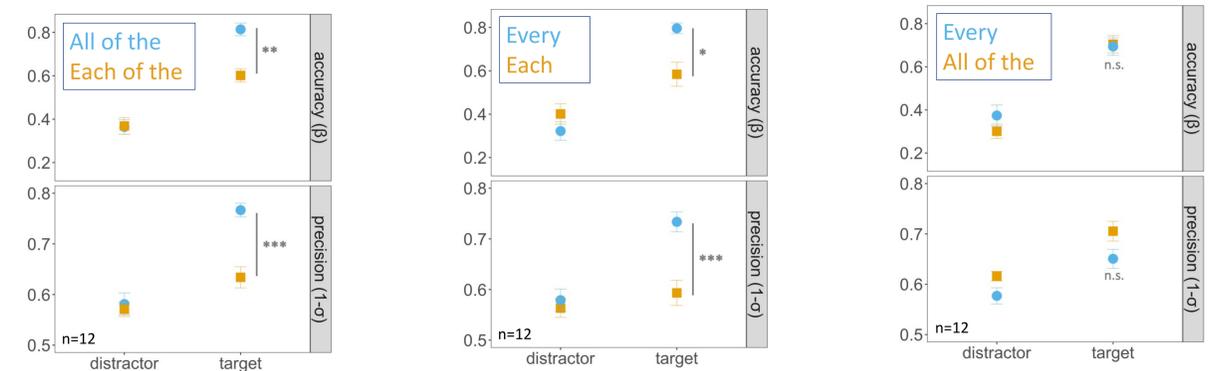
Second-order meaning → attend to & represent sets → encode those sets' cardinalities in memory [4,5]

First-order meaning → attend to & represent individuals → fail to encode set-based properties (e.g., #) in memory

Comparing the universals

Testing truth-conditionally equivalent statements

- Same task, but both conditions were matched in syntax, truth-conditions, and images
 - **Result:** Participants know the restrictor set's cardinality better following *every-* and *all-* statements than following *each*-statements; *every-* and *all-* statements still pattern together when tested within subjects



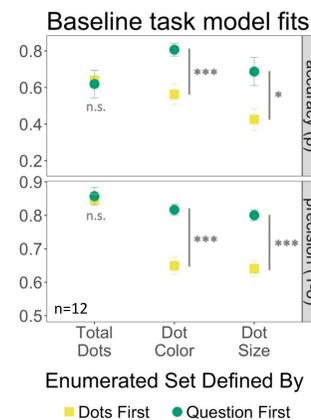
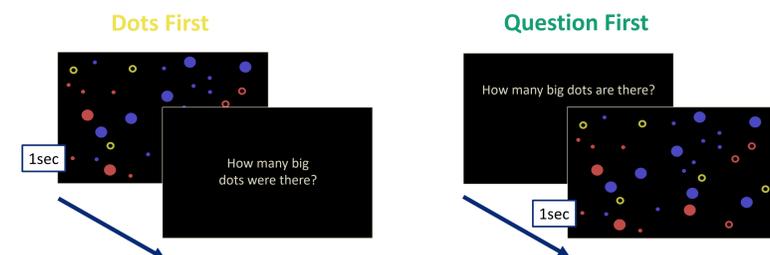
Each-statements lead participants to represent individuals (thanks to their first-order meaning)

Every- and *all-* statements lead participants to leading participants to represent groups (thanks to their second-order meaning)

Background: Measuring cardinality knowledge

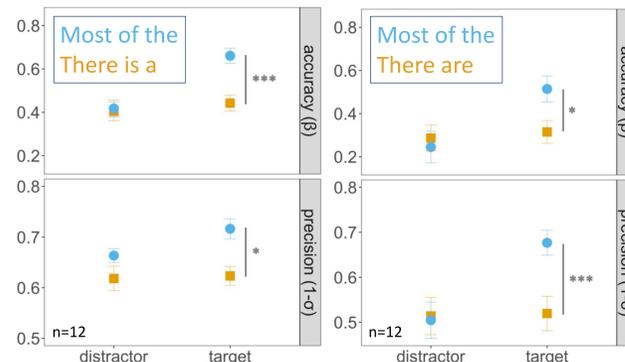
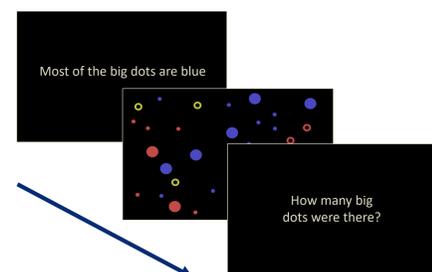
Baseline task

- When asked to estimate the cardinality of some subset, participants can be fit with an accuracy (β) and precision parameter ($1-\sigma$) [6-9]
 - **Result:** Better accuracy & precision when given the question first



Adding language: most- vs. existential-statements

- Participants biased to attend to groups or not based on the statement under evaluation:
 - A decidedly second-order *most*-statement or a plausibly first-order *existential*-statement
 - Follow-up questions probed the restrictor set (target) or a random set (distractor)



- **Result:** Participants know the restrictor set's cardinality better following *most*-statements

Most's second-order meaning leads participants to represent groups

Linguistic consequences of first-order each

Distributivity

- While *every* and *all* can give rise to distributive interpretations, *each* mandatorily does [10,11]:
 - (6) a. Each student sang happy birthday (well as a solo piece / #in perfect harmony)
 - b. Every student/all the students sang happy birthday (well as a solo piece / in perfect harmony)
 - (7) a. Determine whether each dragon is dangerous ('for each dragon, figure out whether it's dangerous')
 - b. Determine whether every dragon is dangerous ('figure out if it's true that every dragon is dangerous')
- *Each* is sometimes said to be a pronunciation of the distributive operator, D (e.g., [12])
 - If *each/D* is first-order, the predicate must to apply to the elements in the domain individually

Genericity

- While *every* and *all* can be used to express generic thoughts, *each* cannot [13,14]:
 - (8) a. #Each bird lays eggs
 - b. Every bird lays eggs
 - c. All birds lay eggs
 - (9) Usually you complain every/#each time we shop
- Generic statements abstract away from individual entities / events and describe group properties
 - FOL considers individuals and their properties
- The # of exceptions tolerated changes with the domain size; hard to capture in FOL (though see [15])
 - The same problem arises for statements with proportional quantifiers, like *most* [16]

Takeaway: each, every, and all are represented in different formats in speakers' minds

- *Each* is represented in a first-order format; *every* and *all* are represented in second-order formats
- Knowledge of group-based properties (e.g., #) following evaluation reflects this subtle difference in meaning

References: [1] Pietroski, Lidz, Hunter, & Halberda (2009) The meaning of 'most': Semantics, numerosity and psychology [2] Lidz, Pietroski, Halberda, & Hunter (2011) Interface transparency and the psychosemantics of most [3] Tomaszewicz (2011) Verification strategies for two majority quantifiers in polish [4] Ariely (2001) Seeing sets: Representation by statistical properties [5] Alvarez (2011) Representing multiple objects as an ensemble enhances visual cognition [6] Stevens (1964) Concerning the psychophysical power law [7] Laming (1997) The measurement of sensation [8] Odic, Im, Eisinger, Ly, & Halberda (2016) Psimle: A maximum-likelihood estimation approach to estimating psychophysical scaling and variability more reliably, efficiently, and flexibly [9] Halberda, Sires, & Feigenson (2006) Multiple spatially overlapping sets can be enumerated in parallel [10] Vendler (1962) Each and every, any and all [11] Dowty (1987) Collective predicates, distributive predicates, and all [12] LaTerza (2014) Distributivity and plural anaphora [13] Beghelli & Stowell (1997) Distributivity and negation: The syntax of each and every [14] Gil (1992) Scopal quantifiers: some universals of lexical effability [15] Asher & Morreau (1995) What some generic sentences mean [16] Rescher (1962) Plurality Quantification
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